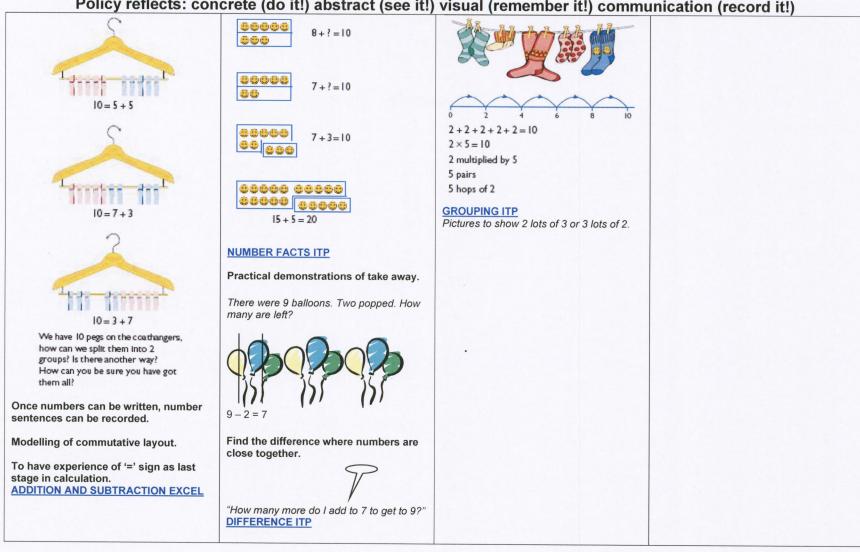
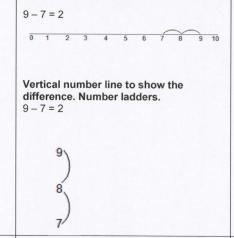
Randlay Primary School and Nursery Calculation policy Stages A & B Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) com

Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) communication (record it!)			unication (record it!)
Addition	Subtraction	Multiplication	Division
Stage A	Stage A	Stage A	Stage A
Counting objects, partitioning and recombining sets using practical apparatus.	Know that the number gets smaller because objects have been removed from the set.	Jumping along number lines in jumps of 1, 2, 5 & 10.	Counting on and back in steps of 1, 2, 5 and 10.
Understand that the number gets bigger.	Practical models of subtraction	Repeated addition, practical demonstrations. (Models and Images charts)	Sharing equally and halving objects in practical contexts.
Addition is commutative.	Counting back on fingers, orally, number lines.	Doubles and grouping	Pictorial recording.
Use number tracks to develop counting	Find the difference, counting on.	Grouping is a random arrangement of a quantity into equal groups.	Grouping, in practical contexts.
skills, forwards and backwards.	MODELS AND IMAGES CHARTS	quantity into equal gloups.	GROUPING ITP
COUNTING ITP Pictorial recording of practical experiences.	(To be used for lots of oral examples)	Arrays are a rectangular arrangement to show the equal groups.	Use cross curricular links (PE) and purposeful objects such as sock and shoes/ animals in the ark to get into groups.
Teacher modelling of number sentences and addition as commutative.	Sing mile	15 15 15	Sharing models such sharing an apple or a Satsuma.
	5+?=10 10-5=?		How many cars can you make if you have 8 wheels?
1+1=2 $2-1=1double 1 is 2 half of 2 is 1$	Los las	This is an array	
公园 医子	6+?=10 ?+6=10 10-6=? 10-4=6	Use of arrays to show that multiplication is commutative. Changing the order does not affect the answer.	MAMA
2+2=4 $4-2=2double 2 is 4 half of 4 is 2$	Lus Lus	Peg boards are a useful model. Use the language of 'lots of', 'groups of' and 'sets of' for 'x'.	
	9+?=10 ?+9=10 10-9=? 10-?=9		



Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) communication (record it!)



Stage B Stage B

Key skills of knowing number bonds to 10 and within 20.

Develop knowledge of fact families, e.g. 2, 5, 7.

000000 00	7=5+2	2+5=7
	7-2=5	7-5=2

EXCEL ADDITION AND SUBTRACTION TRIOS

Counting forwards and recording on a number line.

All answers to be recorded in a number sentence following any informal recording.



Subtraction sentences and jumps (backwards for take away – left and forwards for difference – right) along number lines.

EXCEL ADDITION AND SUBTRACTION TRIOS

Check with the inverse. Understand the effect of adding and subtracting zero

Know that 6 can be thought of as 5 and 1



is 5 and 1 more

Stage B

Pictorial repeated addition. Grouping is a random arrangement of a quantity into equal groups.

Arrays are a rectangular arrangement to show the equal groups.

Stage B

With practical equipment:

Counting on and back in 2s, 5s and 10s and begin counting in 3s.

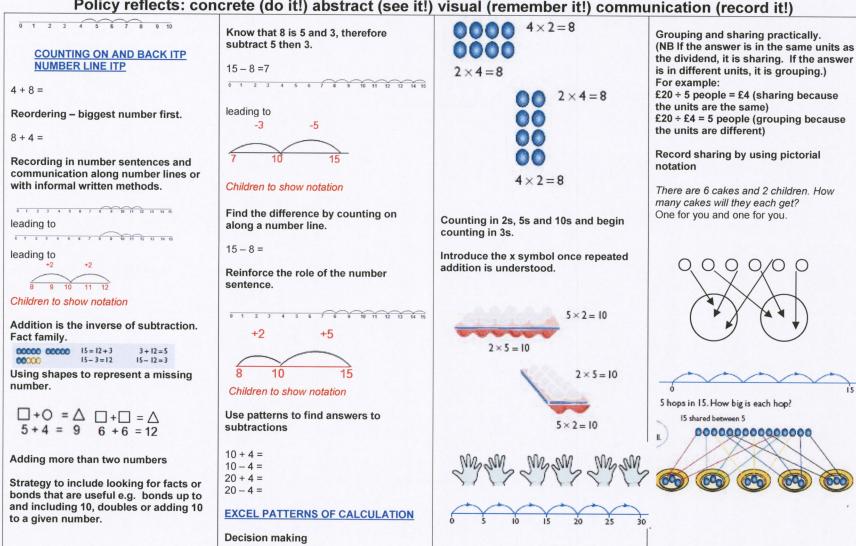
Grouping as repeated addition along the number line.

Introduce the ÷ symbol once repeated addition (grouping) is understood.

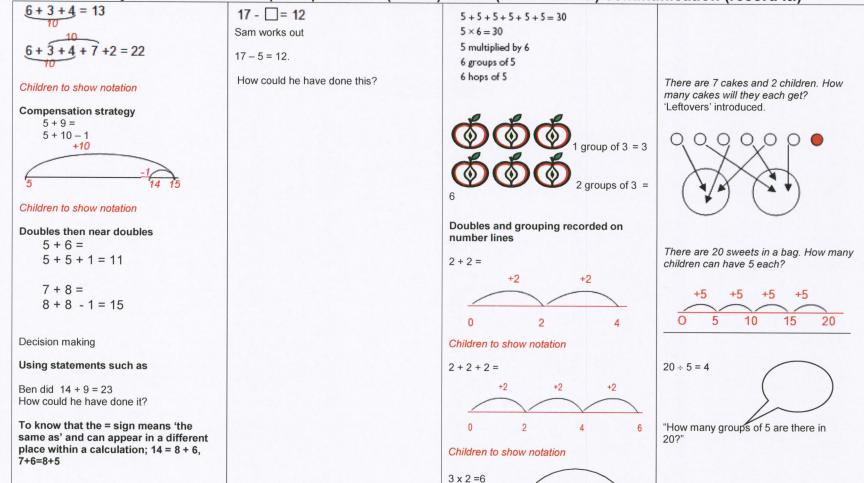
GROUPING ITP

If I have got 4, how many groups of 2 have I got?





Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) communication (record it!)



3 multiplied by 2 equals 6. 3 times 2 equals 6

Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) communication (record it!) Finding simple fractions of quantities. Finding half of 10 apples. In the example above with 5 rows and 9 columns, when you select to count along the columns the given calculation is: $5 \times 9 = 45$ [the 5 is multiplied by 9].

Selecting to count along rows gives: $9 \times 5 = 45$ [the 9 is multiplied by 5].

Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) communication (record it!)

Addition Subtraction Multiplication Division Stage C (Y2/3) Stage C Stage C Stage C Emphasis on mental calculation. Using tables facts 2s, 10s and 5s and Understand division as repeated addition, Place value, partitioning and recombining. begin 3s and 4s. grouping. Combining sets to make a total. Be able to partition a 2 digit number. Rearranging of numbers so Table facts (see multiplication). Progression in use of informal recording that 36 can be seen as 30 and 6 including the number line. MULTIPLICATION BOARD ITP Division facts corresponding to the 2, 10, or as 20 and 16. 5, 3 and 4 times tables. Answers to be recorded as part of a MULTIPLICATION TABLES ITP number sentence. Partitioning of numbers into T and U then Use x and ÷ signs. HTU. Know what each digit represents. Doubles are same as x2. Reordering strategy. MULTIPLICATION AND DIVISION TRIOS TU - TU Vocabulary of double, multiply, groups of, **SPREADSHEET COUNTING ON AND BACK ITP** HTU - TU sets of, lots of etc. **NUMBER LINE ITP** Count a handful of beads by grouping them in Adding: Partitioning strategy for doubling. fives. How many groups of 5 are there? TU + TU = TU How many are left? Can you write a division and when secure moving on to Double 35 sentence to describe this? TU + TU = HTU HTU +TU = HTU How many lengths of 6 m can you cut from 48m of rope? Write the number fact that 24 + 5830x2 5x2 represents this. How did you work it out? ******** (OVERCOMING BARRIERS L2-L3 knowing and using number facts) 54 = 50 + 4 50+4=54 Record using the correct division symbol. 40 + 14 = 54 adding in 10s and 1s A lolly costs 21p. How much do 3 cost? Use of number lines to record repeated addition. +20 PLACE VALUE ITP Partitioning the second number strategy Practical apparatus to support concept. Introduce the vocabulary of remainder. 76 - 43 =76 - 40 = 36add 20, bridge the 10 Practical contexts to be used so that the 36 - 3 = 33+20 calculation is not in the abstract. When it is a subtraction calculation, underline the second number - this is the only number **Decision making** that can be partitioned. Children investigate statements and solve word problems using appropriate methods 73 - 46 =such as mental/ jottings/ numberline.

Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) communication (record it!)

add 20 and then 4

Record partitioned steps in number sentences underneath each other and add mentally.

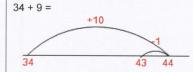
24+58= 20+50=70 4+ 8=12 70+12=82

Introduce column addition without crossing the boundary

24 (20+4) +<u>53 (50+3)</u> <u>77 (70 + 7)</u>

Check answers by repeating addition in different order or by an equivalent calculation.

Compensation strategy



Near doubles

13 + 14 =

Double 14 = 28

28 - 1 = 27

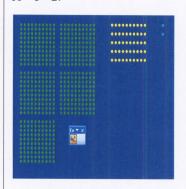
or

Double 13 = 26

26 + 1 = 27

EXCEL MISSING SIGNS AND NUMBERS



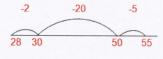


PLACE VALUE DOTS EXCEL SPREADSHEET

Counting back (left) from the larger number in partitioned steps of the smaller number to reach the unknown.

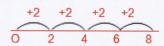
55 – 27 Rearranging strategy Partitioning the 27 into 20, 5 and 2.





or

Grouping



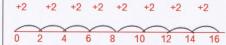
"How many groups of 2 are there in 8?"

The number of jumps tells you the number of groups.

DOUBLING AND HALVING SPREADSHEET

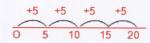
16 ÷ 2 =

"How many groups of 2 are there in 16?" "I know that dividing by 2 is the same as halving."

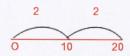


Jump size depends on knowledge and confidence of child. (See D)

 $20 \div 5 =$



4 jumps or moving away from + notation



2 double jumps because 5x2 =10

Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) communication (record it!)

Adding zero leaves a number unchanged/ adding ten to a number keeps units digit constant.

Decision making (mental, jottings, numberline)
Statements and word problems.

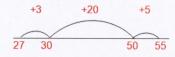


55 - 27 = 28

Find the difference (counting on to the right) Model with numbers that are close together.

$$55 - 27 = 28$$

"How many more do I need to add to 27 to get to 55?"



Subtract mentally pairs of multiples of 10 and 100, using known facts

$$60 - 20 = 40$$
 because $6 - 2 = 4$

$$700 - 300 = 400$$

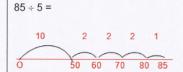
Continue to use the vertical number line.

Use of apparatus (Diennes) to understand rearrangements, e.g. 55 as 40 and 15, not as part of calculations.

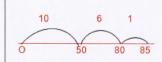
<u>BEADSTICKS ITP</u> to be used with Diennes to develop concept of exchange.

(Beadstick and other place value ITPS)

Decision making Statements and word problems.



or



Decision making

Children investigate statements and solve word problems using appropriate methods such as mental/ jottings/ numberline.

Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) communication (record it!)

Stage D (Y3/4)

Counting on in multiples of 100s, 10s or units using a number line.

HTU + TU Cross the 10s/100s boundary.



NUMBER BOARDS (all stages onwards) for range of numbers

Start with least significant digit

"7 add 4 equals 11 and 60 add 20 equals 80. 1+ 0 = 1 and 1 ten + 8 tens = 9 tens"

All language in the context of the place value and the mental addition of the totals to be done in any order.



Stage D

Counting backwards and forwards beyond zero, negative and positive numbers. (Y4)

-5 is negative 5 and minus 5

TU – TU, HTU – TU, HTU – HTU.

Lead on to decomposition method in expanded format.

Ensure understanding of number partitioning and exchange.

Least significant digit is always dealt with first to establish if the exchange is needed.

Check for mental approach first before written method. "Can I do this in my head?"

NUMBER BOARDS (all stages onwards) for range of numbers

Partitioning the second number strategy

783 – 356 Partitioning the 356 into 300, 50 and 6.



783 - 356 = 427

Difference strategy

"How many more do I need to get from 356 to

Stage D

Known table facts 2, 3,4,5,6, 8 and 10. Use doubling to connect the tables, eg the 4s are doubled to make the 8s.

NUMBER DIALS ITP

Refer to multiplication tables ITPs above.

Refer to Page 60 Overcoming barriers L2-L3 for further guidance.

Multiply by 10 / 100, understanding the shift in the digits.

Know what each digit represents, partition a three digit number.

Commutative law (the principle that the order of two numbers in a multiplication calculation makes no difference, e.g. 5x7=7x5).

MOVING DIGITS

Consolidate arrays and repeated addition. Recalling facts.

 $4 \times 5 = 20, 5 \times 4 = 20.$

Informal recording of partitioned numbers $15 \times 5 = 75$

 $27 \times 3 = 81$

"20 multiplied by 3 equals 60 and 7

Stage D

Understand division as repeated addition.

Know all corresponding tables facts for 2, 3,4,5,6, 8 and 10.

Know what each digit represents in a HTU number.

Use numbers that will generate remainders. r notation for the remainder.

$$21 \div 5 = 4 \text{ r } 1$$

Record using a number line, $30 \div 5 = 6$

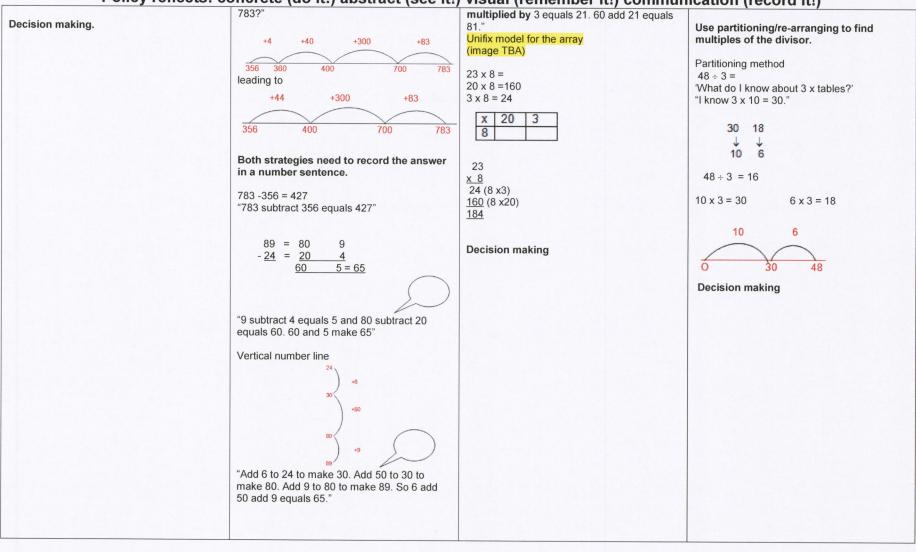


"What do I know about the number I am dividing by?"

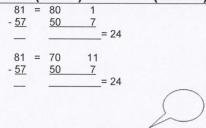
" I know that 5 x 6 = 30"

Repeated addition along a number line with jumps representing number of groups.





Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) communication (record it!)



"1 to subtract 7 is tricky so I will rearrange 81 into 70 and 11. 11 subtract 7 equals 4 and 70 subtract 50 equals 20. 20 and 4 make 24."

BEADSTICKS ITP

Decision making

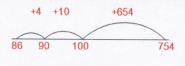
Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) communication (record it!)

Addition Subtraction Multiplication Division Stage E **Stage E** (Y4/5) Stage E Stage E Continue with HTU + HTU, then extend to ThHTU + ThHTU. HTU - TU, then HTU - HTU. Know table facts up to 12 x 12 Know division facts corresponding to (ThHTU - ThHTU) tables up to 12 x 12 Approximate using the most significant (THHTU - HTU) Approximate first. digit, rounding skills. Approximate first using multiplication Partitioning / distributive law, e.g. 28x4 Check using the inverse. Extend to simple decimals with or can be split up into 25x4 add 3x4 or without exchange from pence to 30x4 subtract 2x4. Divide any integer up to 1000 by 10. Refer to the carried digit as a ten or a pounds. hundred. Distributive Law more ... Ensure that all calculation is checked The Distributive Law says that multiplying a number by a group of numbers added together is the same as doing each multiplication separately before started for any other possible 587 "900 ÷ 10 = 90 because the digits move 'tricky' bits. + 475 one place to the right" Example: $3 \times (2 + 4) = 3 \times 2 + 3 \times 4$ 1062 Ensure that the setting out is accurate. So the "3" can be "distributed" across the "2+4" into 3 times 2 and 3 times 4. 11 MOVING DIGITS ITP "7 add 5 equals 12. That's 2 units and 1 754 - 86 = 668ten to carry over. Recap the finding of remainders on the 80 add 70 equals 150 and the one ten to Take away (left) number line first. carry makes 160. That's 6 tens and 100 to carry over. 500 add 400 equals 900 and 21 ÷ 5 the one hundred to carry makes 1000" Pupils to explain the effect of 7648 multiplying by 10 and 100. + 1486 14 "What do I know? I know that 21 is not a or Addition to be done mentally. 120 multiple of 5, so there will be a 1000 HTU and TU x U. remainder." +8000 668 670 9134 $21 \div 5 = 4r1$ Record using grid notation and -80 -6 expanded short multiplication. 7648 + 1486 346 x 9 20 21 9134 111 300 40 Jump size depends on knowledge and confidence of child. (See D) Find the difference (right) This could also be shown as jumps of +5 along the number line resulting in 4 jumps

Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) communication (record it!)

12.45	
7.36	
+ 24.50	
0.11	
1.20	
13-00	
30.00	
44 31	
NUMBER E	<u> 30</u>

ARDS



Decomposition (Continue with Diennes and/or money as appropriate)

"It's tricky to take 6 from 4 and 80 from 50. I need to rearrange the number. I will exchange one ten from 50 which leaves 40 and makes 14 in the units, 40 to subtract 80 is tricky. I will exchange one hundred from 700 and make 140. 14 subtract 6 equals 8. 140 subtract 80 equals 60 and 600 subtract 0 equals 600."

Decomposition

Short multiplication with compact notation to be introduced once the expanded method is secure.

Decision making Children investigate statements and solve word problems using appropriate methods. Children are also given examples of x9 and encouraged to think about using methods such as x10 and subtracting x1.

and a remainder of 1.

Use problems in contexts that require the answer to be rounded up or down following the remainder.

Eg 35 children to sleep four to a tent. How many tents do we need?

Continue to use partitioning/rearranging method.

$$69 \div 3 =$$

'What do I know about 3 x tables?' "I know $3 \times 10 = 30$."

$$30 \div 3 = 10$$

 $30 \div 3 = 10$
 $9 \div 3 = 3$
 $69 \div 3 = 23$

Fractions relate to division. ÷ 4 is the same as halve and halve again.

Recognise that division is noncommutative.

Know that a number cannot be divided by 0.

Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) communication (record it!) 141
Division as repeated subtraction/addition of multiples of the divisor. 132 ÷ 3 Write a partial table 3 x 10 = 30 3 x 20 = 60 3 x 40 = 120 Number line subtraction

Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) communication (record it!)

Stage F (Y5)

Add with increasingly large numbers using the compact method.

Extend methods to include decimals to two decimal places.

Stage F

Subtract with increasingly large numbers using the compact method.

Extend methods to include decimals to two decimal places.

Stage F

Th HTU, HTU, TU x TU and U

28 x 27

X	20	8
20		
7		

Addition to be done mentally or across followed by column addition

28 x 27 56 (7x8) 140 (7 x20) 160 (20x8) 400 (20x20) 756

Long multiplication with compact notation to be introduced once the expanded method is secure.

Stage F

Know division facts corresponding to tables up to 12 x 12 and be able to apply them.

Use the relationship between multiplication and division.

Extend chunking (subtraction/addition of multiples of the divisor, towards the dividend) method to include ThHTU by U, with an integer remainder.

Dividing up to 10,000 by 10/100.

Check with inverse operation. Use of calculator.

Use the number line to find remainders and express the quotient as a fraction or decimal.

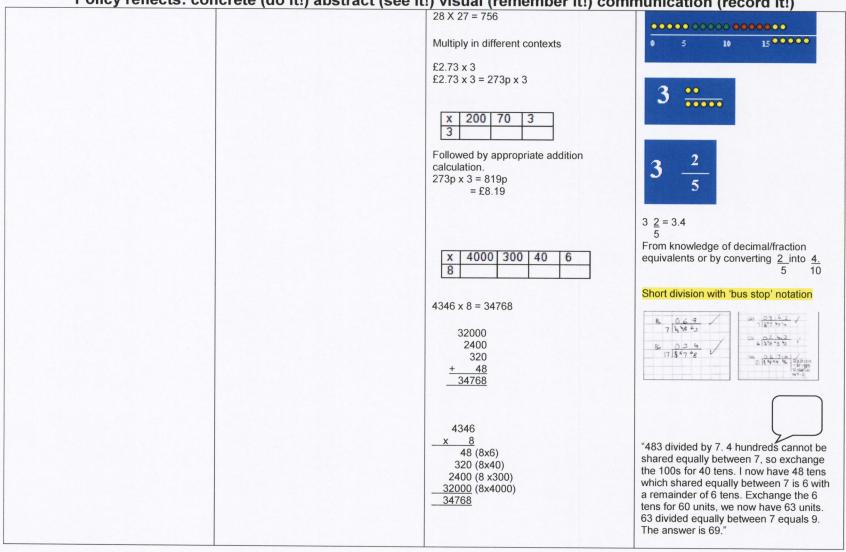
DIVISION WITH REMAINDERS PPT

(example given below)

17 ÷ 5

"What do I know? 17 is not a multiple of





Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) communication (record it!)				
		Decision making Children investigate statements and solve word problems using appropriate methods. Children investigate alternative methods such as compensation strategies and doubling and halving and discuss when these might be most appropriate and efficient. Examples: 24x99 could be done using the grid	Use Diennes or place value equipment to model. Decision making	
		method, but could also be calculated by x100 and subtracting 24x1. 24 x25 could be done using the grid method, but could also be calculated by 24x100, halving to find x50 and halving again to find x 25. or using doubling and halving, 24 x25=12x50 =6 x100	(OVERCOMING BARRIERS Level 4 to Level 5 – Questions.) Word problems, e.g. 200 people attended a concert. ¹ / ₅ of the people had complimentary tickets. The rest paid £7.50 each. How much money was collected from selling tickets? Money and measures, e.g. Which is longer: ³ / ₄ of an hour or 2500 seconds? Partitioning method for HTU.	
			847 ÷ 7 "What do I know? I know 7x12 = 84 so 7 x120 = 840" 840	

Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) communication (record it!)				
			Peter says that, if you want to divide a number by 12, you can divide it by 4 then by 3. Is he right? Explain how you know. Work out 768 ÷ 12 using Peter's method and using another method. Do you get the same answer?	
			How many 35p packets of stickers can I buy with £5? Explain how you know.	
			Coaches have 56 seats for passengers. How many coaches are needed to take 275 people on a trip?	
			Complete this calculation: 943 ÷ 41 = 2	
			Work out whether or not 29 is a factor of 811.	

Addition	Subtraction	Multiplication	Division
Stage G (Y6)	Stage G	Stage G	Stage G
Promote decision making so that pupils choose an appropriate method/strategy. Continue the use of informal methods and number lines.	ThHTU – ThHTU then any number of digits. Appropriate use of a calculator including interpretation of displays.	ThHTU x TU and HTU x TU and including decimals. TU x TU	Know all multiplication facts and corresponding division facts to 12 x 12 and beyond and be able to apply them. Explain the effect of dividing by1000.
Ensure understanding of standard written method. Continue ThHTU + ThHTU then calculations with any number of digits. Approximate using the most significant digits and a feel for the 'whole' number. Appropriate teaching/use of the calculator including interpreting the display, e.g. money or measures. Calculator display 0.37 is then interpreted as 37p in the context of money. Remind 4p = 0.04 Calculator display £1.4 is interpreted as £1.40 7648 + 1486 9134 111 Decimal points are fixed on the line with digits in the squares. Decimals, fill 'empty columns' with zeros.	Money, measures and real life contexts. 6467 - 2684 5131 8467 - 2684 - 3783 3249 - 7:25 11 81 324:900 - 7:25 317:65 13 6 - 28 = +02 +106 28 3 136	78 x42 16 (2 x 8) 140 (2 x 70) 320 (40 x 8) +2800 (40 x 70) 3276 Compact (long) 78 x42 156 +3120 3276 Involve decimals, money and measures through approximation and appropriate use of the calculator. Addition either mentally or by column addition.	Extend methods to include Th HTU by TU. Continue to use the short division method when the two digit divisor is up to 12 or is a easily recognisable multiple eg 20, 25 or 50. Use a calculator appropriately, approximating first. Use of calculator for interpreting the quotient by entering a fraction to find the decimal equivalent. Mathsonline.org-long division Use long division only with pupils who are secure with number sense and place value. 384 ÷ 16 "What do I know about the divisor?" Record partial
	136 – 28 = 108		tables.

Tolloy Tolloots.	concrete (do it!) abstract (see	iti) visuai (reilielliber iti) collili	iunication (record it!)
1249 + 725 12490 + 725 13215 11	leading to 146 - 276 +004 +02 +116 276 280 3 146	Decimals. Teach children how to use known facts to build new facts according to the place value required, e.g. $3x4 = 12$ $3x0.4 = 1.2$ $3x0.04 = 0.12$	
		0.75×6 $0.7 \times 6 = 4.2$ $0.05 \times 6 = 0.3$ $0.75 \times 6 = 4.5$ Grid method based upon very secure place value. $\begin{array}{ c c c c c c c c c c c c c c c c c c c$	Long division (thinking not generally recorded) 24 16) 38 ⁶ 4 (38÷16=2 r 6; 2x16=32) - 32 √ (bring the 4 down) 64 (16 into 64=4; 4x16=64) - 64 0 (no remainder) Continue to make use of partitioning and the number line for repeated addition where appropriate. 944 ÷ 22 = What do I know about the divisor? Express the remainder as a fraction or decimal. Overcoming Barriers L4/5 Division giving a decimal answer, e.g. Divide 9 by 5 giving your answer as a decimal. Missing number calculations, e.g.

Policy reflects: concrete (do it!) abstract (see it!) visual (remember it!) communication (record it!)]÷ 8 = 0.04; 0.1 30 60 0.5 Which is closer to 100: 5.2 × 17 or 7.2 × 15? Use written methods to prove your answer.